

Jacobi's method of successive 2D rotations

After 0 rotations: 0.303834 = off-diag. rms

$$A = \begin{bmatrix} 1.0000 & \underline{0.5000} & 0.3333 & 0.2500 \\ \underline{0.5000} & 0.3333 & 0.2500 & 0.2000 \\ 0.3333 & 0.2500 & 0.2000 & 0.1667 \\ 0.2500 & 0.2000 & 0.1667 & 0.1429 \end{bmatrix} \quad V = \begin{bmatrix} 1.0000 & 0.0000 & 0.0000 & 0.0000 \\ 0.0000 & 1.0000 & 0.0000 & 0.0000 \\ 0.0000 & 0.0000 & 1.0000 & 0.0000 \\ 0.0000 & 0.0000 & 0.0000 & 1.0000 \end{bmatrix}$$

After 1 rotations: 0.225051 = off-diag. rms

$$A = \begin{bmatrix} 1.2676 & 0.0000 & \underline{0.4119} & 0.3148 \\ -0.0000 & 0.0657 & \underline{0.0631} & 0.0584 \\ \underline{0.4119} & 0.0631 & 0.2000 & 0.1667 \\ 0.3148 & 0.0584 & 0.1667 & 0.1429 \end{bmatrix} \quad V = \begin{bmatrix} 0.8817 & -0.4719 & 0.0000 & 0.0000 \\ 0.4719 & 0.8817 & 0.0000 & 0.0000 \\ 0.0000 & 0.0000 & 1.0000 & 0.0000 \\ 0.0000 & 0.0000 & 0.0000 & 1.0000 \end{bmatrix}$$

After 2 rotations: 0.149590 = off-diag. rms

$$A = \begin{bmatrix} 1.4080 & 0.0204 & 0.0000 & \underline{0.3517} \\ 0.0204 & 0.0657 & 0.0598 & 0.0584 \\ 0.0000 & 0.0598 & 0.0596 & 0.0562 \\ \underline{0.3517} & 0.0584 & 0.0562 & 0.1429 \end{bmatrix} \quad V = \begin{bmatrix} 0.8345 & -0.4719 & -0.2845 & 0.0000 \\ 0.4466 & 0.8817 & -0.1523 & 0.0000 \\ 0.3227 & 0.0000 & 0.9465 & 0.0000 \\ 0.0000 & 0.0000 & 0.0000 & 1.0000 \end{bmatrix}$$

After 3 rotations: 0.041928 = off-diag. rms

$$A = \begin{bmatrix} 1.4992 & 0.0344 & 0.0141 & 0.0000 \\ 0.0344 & 0.0657 & \underline{0.0598} & 0.0514 \\ 0.0141 & \underline{0.0598} & 0.0596 & 0.0544 \\ -0.0000 & 0.0514 & 0.0544 & 0.0516 \end{bmatrix} \quad V = \begin{bmatrix} 0.8078 & -0.4719 & -0.2845 & -0.2095 \\ 0.4323 & 0.8817 & -0.1523 & -0.1121 \\ 0.3124 & 0.0000 & 0.9465 & -0.0810 \\ 0.2510 & 0.0000 & 0.0000 & 0.9680 \end{bmatrix}$$

After 4 rotations: 0.034100 = off-diag. rms

$$A = \begin{bmatrix} 1.4992 & 0.0346 & -0.0134 & 0.0000 \\ 0.0346 & 0.1225 & 0.0000 & \underline{0.0747} \\ -0.0134 & -0.0000 & 0.0028 & 0.0040 \\ -0.0000 & \underline{0.0747} & 0.0040 & 0.0516 \end{bmatrix} \quad V = \begin{bmatrix} 0.8078 & -0.5381 & 0.1187 & -0.2095 \\ 0.4323 & 0.5344 & -0.7176 & -0.1121 \\ 0.3124 & 0.6518 & 0.6863 & -0.0810 \\ 0.2510 & 0.0000 & 0.0000 & 0.9680 \end{bmatrix}$$

After 5 rotations: 0.015256 = off-diag. rms

$$A = \begin{bmatrix} 1.4992 & \underline{0.0293} & -0.0134 & -0.0185 \\ \underline{0.0293} & 0.1697 & 0.0022 & 0.0000 \\ -0.0134 & 0.0022 & 0.0028 & 0.0034 \\ -0.0185 & 0.0000 & 0.0034 & 0.0044 \end{bmatrix} \quad V = \begin{bmatrix} 0.8078 & -0.5667 & 0.1187 & 0.1106 \\ 0.4323 & 0.3917 & -0.7176 & -0.3804 \\ 0.3124 & 0.5076 & 0.6863 & -0.4169 \\ 0.2510 & 0.5174 & 0.0000 & 0.8181 \end{bmatrix}$$

After 14 rotations: λ_2 0.000008 = off-diag. rms \vec{u}_2

$$A = \begin{bmatrix} 1.5002 & 0.0000 & 0.0000 & -0.0000 \\ 0.0000 & \underline{0.1691} & -0.0000 & -0.0000 \\ 0.0000 & -0.0000 & 0.0001 & -0.0000 \\ -0.0000 & -0.0000 & -0.0000 & 0.0067 \end{bmatrix} \quad V = \begin{bmatrix} 0.7926 & -0.5821 & 0.0292 & 0.1792 \\ 0.4519 & 0.3705 & -0.3287 & -0.7419 \\ 0.3224 & 0.5096 & 0.7914 & 0.1002 \\ 0.2522 & \underline{0.5140} & -0.5145 & 0.6383 \end{bmatrix}$$

\log_{10} (r.m.s. off-diag. element)

