

18.04 Problem Set 3

due at lecture Fri 14 Nov 03

- 1 As a sequel to Prob 3 of Exam 2, also use residue calculus to evaluate

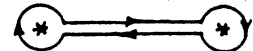
$$I_5 = \int_{-\infty}^{\infty} \frac{dx}{\cosh^5 x}$$

- 2 Evaluate  $\int_{-\infty}^{\infty} \frac{x}{\sinh x} dx$  . HINT:



- 3 Evaluate the integral  $\int_{-\infty}^{\infty} \frac{\sin^3 x}{x^3} dx$  via some trick similar to our friend  $\sin^2 x = \text{Re}(1 - e^{2ix}) / 2$  .

- 4 As in the underlined HW Prob 13 from p.355, use a closed contour shaped about like so to evaluate the integral



$$\int_0^1 (x^2 - x^3)^{-1/3} dx$$

- 5 Solve  $\nabla^2 T = 0$  for that infinite region of the  $x,y$  plane which lies outside the two circles  $|z-i| = 1$  and  $|z+i| = 1$  . The boundary conditions are the  $T = +1$  on the upper circle, and  $T = -1$  on the lower circle. HINT: Consider  $w = 1/z$  .

