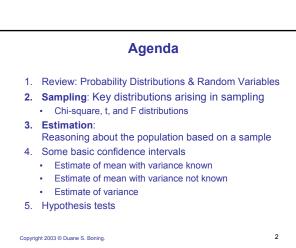
SMA 6304 / MIT 2.853 / MIT 2.854 Manufacturing Systems

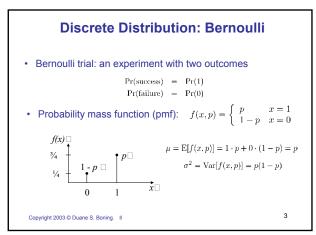
Lecture 9: Statistical Inference

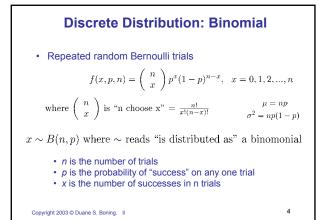
Lecturer: Prof. Duane S. Boning

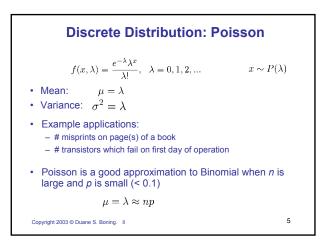
1

Copyright 2003 © Duane S. Boning.







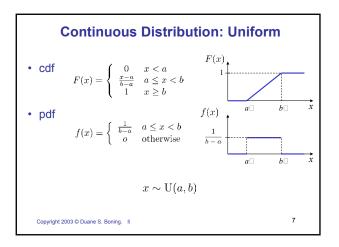


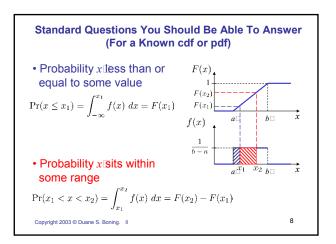


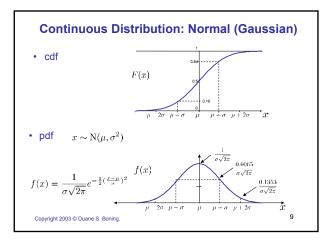
6

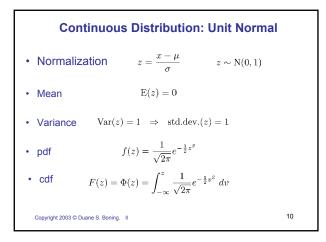
- Uniform Distribution
- Normal Distribution
 - Unit (Standard) Normal Distribution

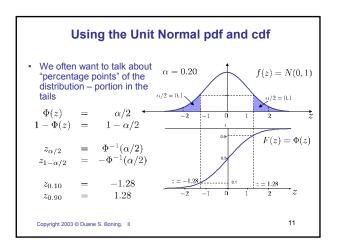
Copyright 2003 © Duane S. Boning. II

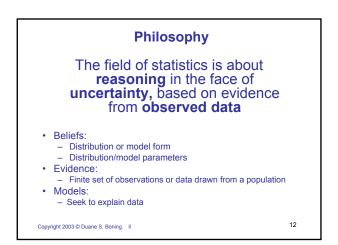


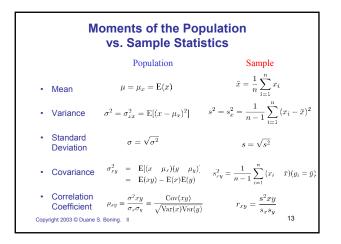


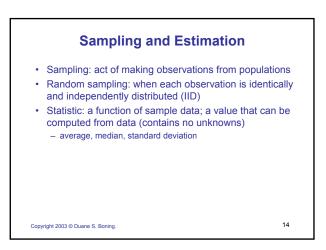


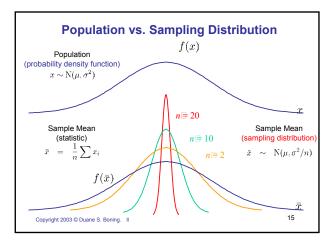


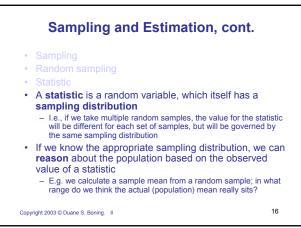












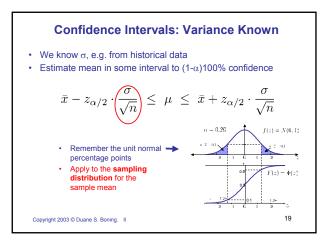
Sampling and Estimation – An Example	
 Suppose we know that the thickness of a part is normally distributed with std. dev. of 10: 	$T \sim N(\mu_{\rm unknown}, 100)$
• We sample <i>n</i> = 50 random parts and compute the mean part thickness:	$\bar{T} = \frac{1}{n} \sum_{i=1}^{n} T_i = 113.5$
• First question: What is distribution of \bar{T} ?	$E(\bar{T}) - \mu$ $Var(\bar{T}) = \sigma^2/n = 100/50$
$ar{T} \sim N(\mu,2)$	$\operatorname{Var}(\overline{T}) = \sigma^2/n = 100/50$ Normally distributed
 Second question: can we use knowledge of <i>T</i> distribution to reason about the actual (population) mean μ given observed (sample) mean? 	
Copyright 2003 © Duane S. Boning. II	17

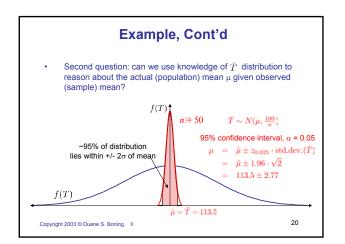


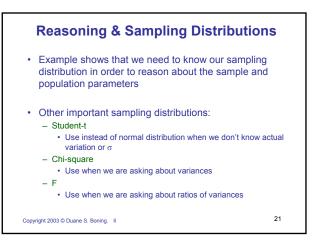
Point Estimation:

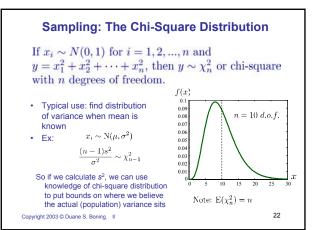
- Find best values for parameters of a distribution
- Should be
 - Unbiased: expected value of estimate should be true value
 - · Minimum variance: should be estimator with smallest variance
- Interval Estimation:
 - Give bounds that contain actual value with a given probability
 - Must know sampling distribution!

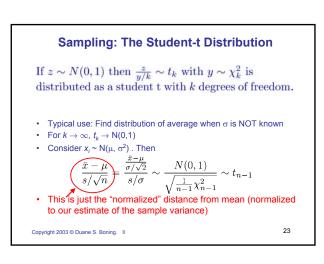
```
Copyright 2003 © Duane S. Boning. II
```

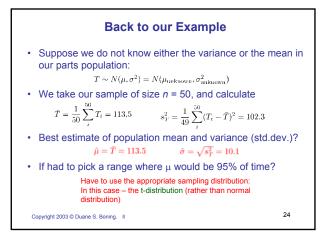


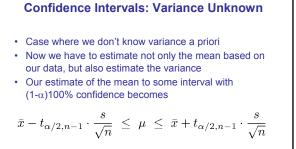








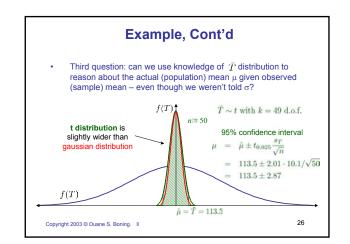


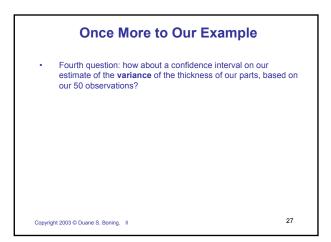


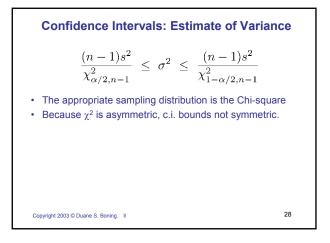
Note that the t distribution is slightly wider than the normal distribution, so that our confidence interval on the true mean is not as tight as when we know the variance.

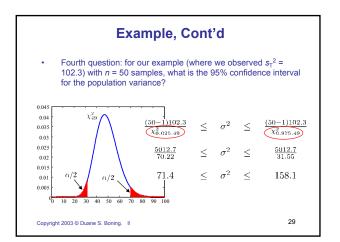
Copyright 2003 © Duane S. Boning. II

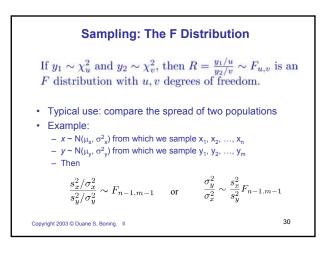
25

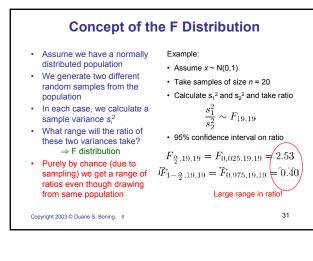


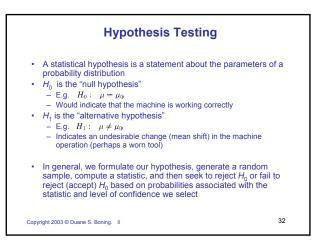


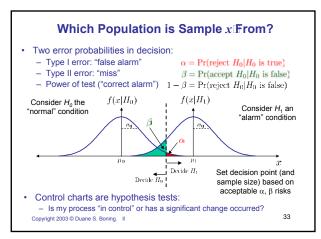












Summary

- Review: Probability Distributions & Random Variables
 Sampling: Key distributions arising in sampling
- Chi-square, t, and F distributions
- 3. Estimation: Reasoning about the population based on a sample
- 4. Some basic confidence intervals
 - Estimate of mean with variance known
 Estimate of mean with variance not known
 - Estimate of mean with variance not know
 Estimate of variance
- 5. Hypothesis tests

Next Time:

- 1. Are effects (some variable) significant? ⇒ ANOVA (Analysis of Variance)
- 2. How do we model the effect of some variable(s)? \Rightarrow Regression modeling

Copyright 2003 © Duane S. Boning. II

34