Lecture Topics

- Announcements, introduction
- Lorentz transformations
- Light-cone coordinates

Reading: Zwiebach, Sections 2.1-2.3

Strings at Many Scales

Classical strings, cosmic strings QCD strings, gluons or flux tubes hold quarks together as qq^+



Flux tube - String of 0.2 fm AdS/CFT Anti-desiltem/conformal field theory

Fundamental Strings Standard model of particle physics, cosmology, inflation Zero thickness, mass, measure

Relativistic Strings

Intervals:

$$(ct,x,y,z)\equiv (x^0,x^1,x^2,x^3)\equiv x^\mu$$

$$\begin{array}{cc}S&S^1\\ \text{Event 1}&x^\mu&x'^\mu\\ \text{Event 1}&x^\mu+\Delta x^\mu&x'^\mu+\Delta x'^\mu\end{array}$$

$$-\Delta s^{2} = -\Delta x^{0^{2}} + \sum_{i} \Delta x^{i^{2}} = g_{\mu\nu} x^{\nu} = x_{\mu} x^{\nu} = -\Delta x^{\prime 0^{2}} + \Delta x^{\prime i^{2}} = -\Delta s^{i^{2}}$$
$$\Delta s^{2} = \Delta s^{i^{2}}$$

$$\Delta s^2 = \begin{array}{c} > 0 & \text{timelike separated} \\ = 0 & \text{lightlike separated} \\ < 0 & \text{spacelike separated} \end{array}$$

Again, the interval:

$$-ds^2 = \eta_{\mu\nu} dx^\mu dv^\nu$$

 $\eta_{\mu\nu}$ symmetric by definition:

$$\eta_{\mu\nu} = \left(\begin{array}{ccc} -1 & & \\ & 1 & \\ & & 1 & \\ & & & 1 \end{array} \right)$$

$$a^{\mu} \to a_{\mu} = \eta_{\mu\nu} a^{\nu} \forall a$$

Given a^{μ} , b^{μ} , $a \cdot b = a^{\mu}b_{\mu} = \eta_{\mu v}a^{\mu}b^{v}$ Inverse metric: $\eta^{\mu v} = (\eta^{-1}_{\mu v})$

$$\eta^{\nu\rho}\eta_{\rho\mu} = \delta^{\nu}_{\mu}(\text{summed over }\rho)$$

$$\eta^{\rho\mu}b_{\mu} = \eta^{\rho\mu}\eta_{\mu\nu}b^{\nu} = \delta\rho_{\nu}b^{\nu} = b^{\rho}$$

Lorentz Transformation:



$$\beta = \frac{v}{c}; \gamma = \frac{1}{\sqrt{1-\beta^v}}$$

$$x' = (x - \beta ct)\gamma$$
$$y' = y$$
$$z' = z$$
$$ct' = \gamma(ct - \beta^{x})$$

$$\begin{aligned} x^{0'} &= \gamma (x^0 - \beta x^1) \\ x^{1'} &= \gamma (-\beta x^0 + x^1) \\ x^{2'} &= x^2 \\ x^{3'} &= x^3 \end{aligned}$$

A linear invertible transform between x^{μ} and x'^{μ} that satisfies $\Delta s^2 = \Delta s'^2$

$$x'^{\mu} = L^{\mu}_{v} x^{v}$$

L is a Lorentz transfer of $L^T\eta L=\eta$

Light cone coordinates:

$$x^{0}, x^{1}, \underbrace{x^{2}, x^{3}}_{\text{Keep these two}}$$
$$x^{+} = \frac{1}{\sqrt{2}}(x^{0} + x^{1})$$
$$x^{-} = \frac{1}{\sqrt{2}}(x^{0} - x^{1})$$
$$x^{\pm} = \frac{1}{\sqrt{2}}(x^{0} \pm x^{1})$$

