18.099 - 18.06CI.

HW-2

Due on Monday, Feb 23 in class. First draft due on Thursday, Feb 19.

- (1) Find the dimension of the space of all homogeneous polynomials of degree p in n variables. Prove your answer. Make sure that it works in both cases $p \le n$ and p > n, as well as for the limit values p = 0 and n = 1.
- (2) Two linear spaces L and M over a field F are isomorphic if there exists a linear map $f: L \to M$ which is a set-theoretical bijection (one-one and onto). Prove that two finite dimensional linear spaces are isomorphic if and only if their dimensions coincide.