

Given: $\rho = 0.5 \rho_{SL}$ $l = 4 l_{SL}$ (characteristic length)
 $a = 0.95 a_{SL}$ (span, chord, whatever)
 $\mu = 0.95 \mu_{SL} \rightarrow$ tunnel quantity

a) To match M_∞ , must have $\frac{V}{a} = \frac{V_{SL}}{a_{SL}} \rightarrow V = 0.95 V_{SL}$

To also match Re , must have $\frac{\rho V l}{\mu} \stackrel{?}{=} \frac{\rho_{SL} V_{SL} l_{SL}}{\mu_{SL}}$

or $\frac{\rho}{\rho_{SL}} \frac{V}{V_{SL}} \frac{l}{l_{SL}} \stackrel{?}{=} \frac{\mu}{\mu_{SL}}$

$0.5 \cdot 0.95 \cdot 4 \stackrel{?}{=} 0.95 \quad \times \quad \underline{\text{not possible}}$

Cannot simultaneously match M_∞ and Re without being able to adjust another parameter (like ρ !)

b) Tunnel quantities: $\rho_T a_T \mu_T V_T l_T$

Unknown: ρ_T

Given: $a_T = a_{SL} = \frac{1}{0.95} a$

$\mu_T = \mu_{SL} = \frac{1}{0.95} \mu$

$l_T = \frac{1}{4} l$

because $T_T = T_{SL}$
as given

Require $M = M_T \rightarrow \frac{V}{a} = \frac{V_T}{a_T} \rightarrow V = 0.95 V_T$

Require $Re = Re_T \rightarrow \frac{\rho V l}{\mu} = \frac{\rho_T V_T l_T}{\mu_T}$

$\rho_T = \rho \cdot \frac{V}{V_T} \frac{l}{l_T} \frac{\mu_T}{\mu} = \rho \cdot 0.95 \cdot 4 \frac{1}{0.95} = 4 \rho$

or $\boxed{\rho_T = 2 \rho_{SL}}$

From equation of state: $\boxed{\rho_T = \rho_{SL} \left(\frac{\rho_T}{\rho_{SL}} \right)^{\uparrow 2} \left(\frac{T_T}{T_{SL}} \right)^{\uparrow 1} = 2 \rho_{SL} = 2 \text{ atm.}}$